



## E 7.1

Binary PAM is used to transmit information over an unequalized linear filter channel. When  $a=1$  is transmitted, the noise free output of the demodulator is

$$x_m = \begin{cases} 0.3 & (m=1) \\ 0.9 & (m=0) \\ 0.3 & (m=-1) \\ 0 & (\text{otherwise}) \end{cases}$$

- a) Design a three-tap zero-forcing equalizer so that the output is

$$q_m = \begin{cases} 1 & (m=0) \\ 0 & (m=\pm 1) \end{cases}$$

- b) Determine  $q_m$  for  $m=\pm 2, \pm 3$  by convolving the impulse response of the equalizer with the channel response.

## E 7.2

Repeat problem (E 7.1) using the MMSE as the criterion for optimizing the tap coefficients. Assume that the noise power spectral density is 0.1W/Hz.

## E 7.3

A time-dispersive channel having an impulse response  $h(t)$  is used to transmit four-phase PSK at a rate  $R=1/T$  symbols/s. The equivalent discrete-time channel is shown in Figure 7.1. The sequence  $\{\eta_k\}$  is white noise sequence having zero mean and variance  $\sigma^2 = N_o$ .

- a) What is the sampled autocorrelation function sequence  $\{x_k\}$  for this channel, where  $\{x_k\}$  defined by

$$x_k = \int_{-\infty}^{\infty} h^*(t)h(t+kT)dt$$

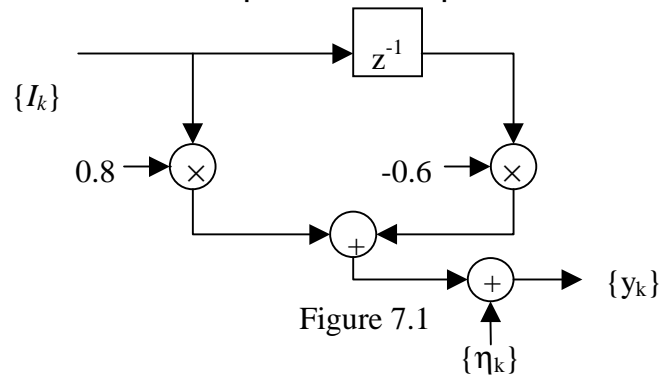
- b) The minimum MSE performance of a linear equalizer and a decision feedback equalizer having an infinite number of taps depends on the folded spectrum of the channel

$$\frac{1}{T} \sum_{n=-\infty}^{\infty} \left| H(\omega + \frac{2\pi n}{T}) \right|^2$$

where  $H(\omega)$  is the Fourier transform of  $h(t)$ .

Determine the folded spectrum.

- Use your answer in (b) to express the minimum MSE of a linear equalizer in terms of the folded spectrum.
- Repeat (c) for an infinite-tap decision equalizer.



## Homework–7 Deadline 08 April 2002 at 10.00

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Homework return box is located at Otakaari 5, 2nd floor, near the E-wing. You can also return the answers to the assistant just before the class.

The real and imaginary parts of the filter coefficients  $\{c_n(i)\}$  as well as the signal phase  $\phi$  at the output of the linear equalizer can be adjusted iteratively towards their optimum values using the steepest descent algorithm,

$$\begin{aligned}\operatorname{Re}\{c_n(i)\} &= \operatorname{Re}\{c_n(i)\} - \Delta \frac{\partial |e_k|^2}{\partial [\operatorname{Re}\{c_n\}]} \\ \operatorname{Im}\{c_n(i)\} &= \operatorname{Im}\{c_n(i)\} - \Delta \frac{\partial |e_k|^2}{\partial [\operatorname{Im}\{c_n\}]} \\ \phi\{i+1\} &= \phi(i) - \Delta_\phi \frac{\partial |e_k|^2}{\partial \phi}\end{aligned}$$

where the error signal is defined as

$$e_k = z_k - \hat{b}_k = \left( \sum_{m=-M}^M c_m r_{k-m} \right) \exp(j\phi) - \hat{b}_k$$

Derive the results given in the handouts by setting this expression of  $e_k$  into the iteration equations shown above.

For definition of variables, please refer to lecture handouts.