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# Overview of MIMO systems

**S-72. 333 Postgraduate Course in Radio Communications**

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## Outline

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- 1.3 MIMO Benefits

### **2 SISO Vs MIMO**

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- 4.2 Non linear receiver (ML, SIC)
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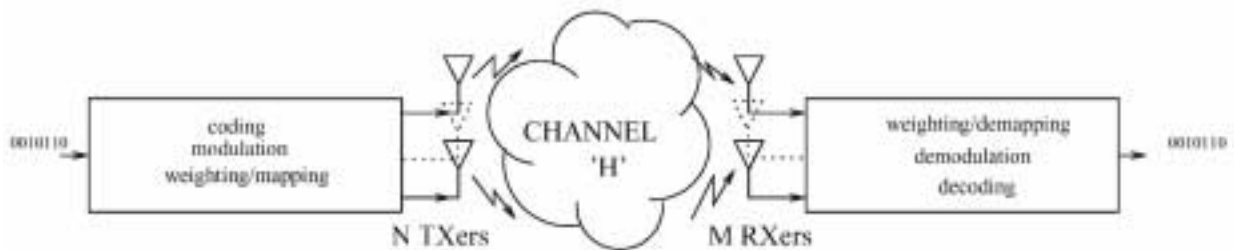
### **5 Space-Time Coding (Transmit / Receive Diversity)**

### **6 Conclusion**

## Multiple-Input Multiple-Output (MIMO) Wireless Systems

### 1.1 What are MIMO systems ?

- A MIMO system consists of several antenna elements, plus adaptive signal processing, at both transmitter and receiver
- First introduced at Stanford University (1994) and Lucent (1996)
- Exploit multipath instead of mitigating it



### 1.2 Wireless channels limitations

#### **Wireless transmission introduces:**

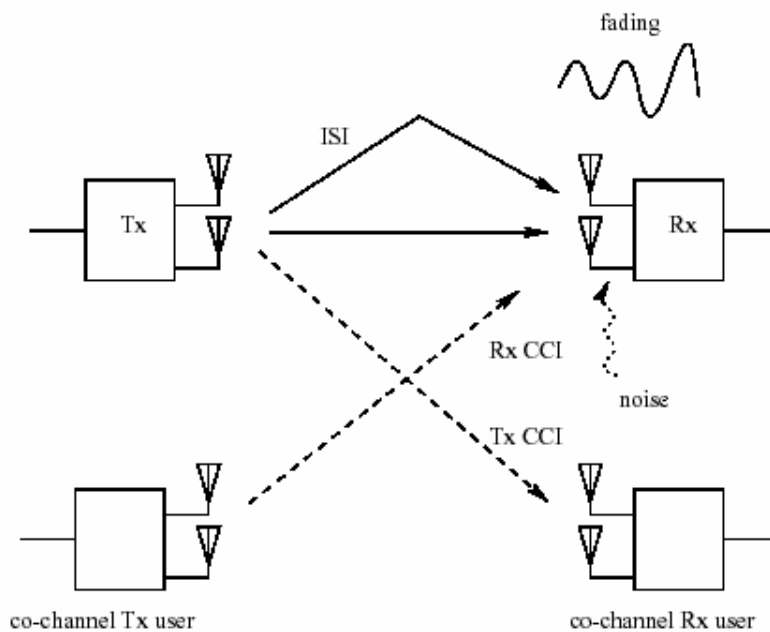
**Fading:** multiple paths with different phases add up at the receiver, giving a random (Rayleigh/Ricean) amplitude signal.

**ISI:** multiple paths come with various delays, causing intersymbol interference.

**CCI:** Co-channel users create interference to the target user

**Noise:** electronics suffer from thermal noise, limiting the SNR.

## Wireless channels limitations : summary



### 1.3 MIMO Benefits :

- higher capacity (bits/s/Hz)  
(spectrum is expensive; number of base stations limited)
- better transmission quality (BER, outage)
- Increased coverage
- Improved user position estimation

#### Due to :

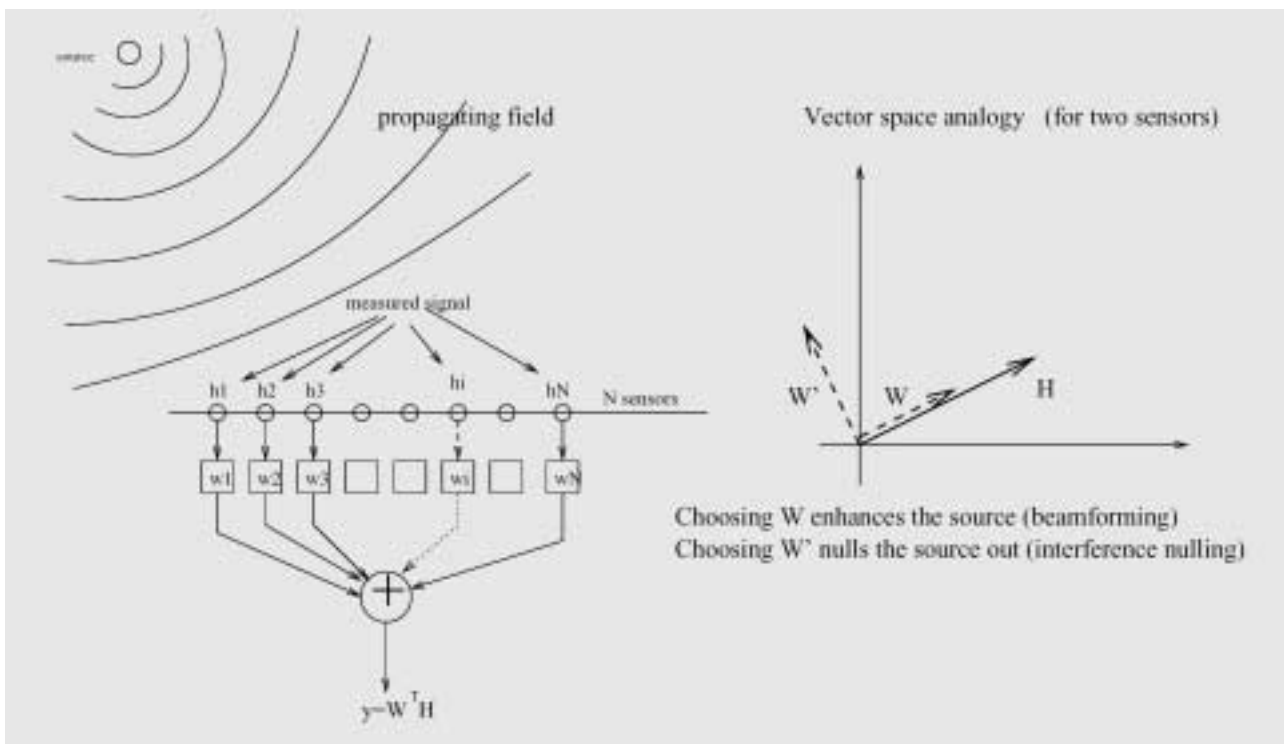
- **Spatial multiplexing gain** : Capacity gain at no additional power or bandwidth consumption obtained through the use of multiple antennas at both sides of a wireless radio link
- **Diversity gain** : Improvement in link reliability obtained by transmitting the same data on independently fading branches
- **Array gain**
- **Interference reduction**

**Array gain principle :**

The array gain is defined by the gain in mean SNR

$$\overline{SNR} = \frac{(E|h_1|^2 + \dots + E|h_N|^2)\sigma_s^2}{\sigma_n^2} = N \frac{E|h|^2\sigma_s^2}{\sigma_n^2} = N\overline{SNR}_{input}$$

↳ The output SNR is  $N$  times the input SNR

**Receiving data over N antennas :**

## 2 SISO Vs MIMO

### Capacity of SISO Systems (1 by 1)

At fixed time  $t$ , the SISO channel is an additive white Gaussian noise (AWGN) channel with capacity :

$$C(t) = \log_2(1 + \text{SNR}_{\text{siso}}(t)) \text{ Bit/Sec/Hz}$$

where  $\text{SNR}_{\text{siso}}(t)$  is the *received* signal to noise ratio at time  $t$  :

$$\text{SNR}_{\text{siso}}(t) = \frac{|h(t)|^2 \sigma_s^2}{\sigma_n^2}$$

➔ +3dB of extra power needed for one extra bit per transmission !

### Capacity of MIMO systems

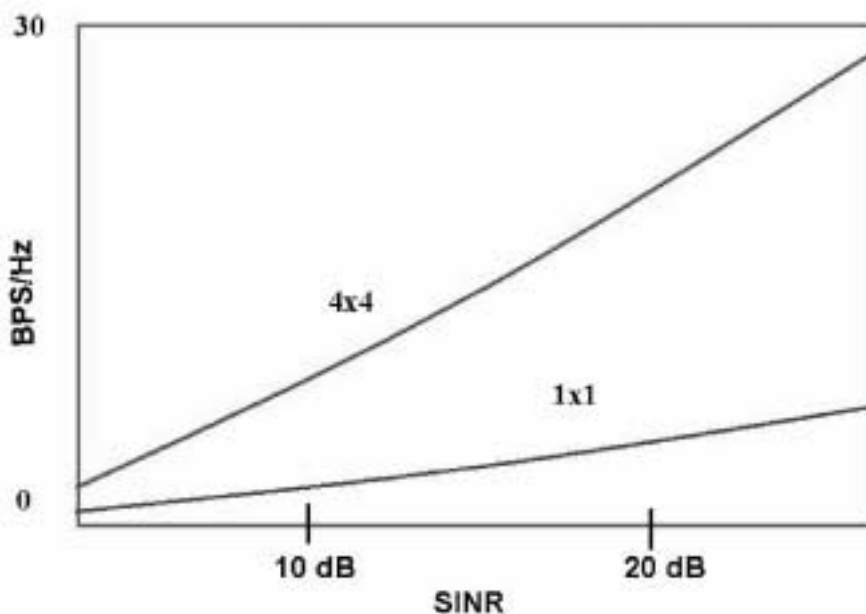
Note: we assume channel unknown at transmitter

$$C_{\text{erg}} = \mathcal{E}_H \left( \log_2 \left[ \det \left( I_M + \frac{\rho}{N} \mathbf{H} \mathbf{H}^* \right) \right] \right) \approx \alpha \min(M, N)$$

where  $\mathbf{H}$  is the  $M \times N$  random channel matrix and  $\rho$  is the average signal-to-noise ratio (SNR) at each receiver branch.

➔ Capacity proportional to min of # TX and # RX antennas!

**Comparison : Average capacity of ideal MIMO systems**

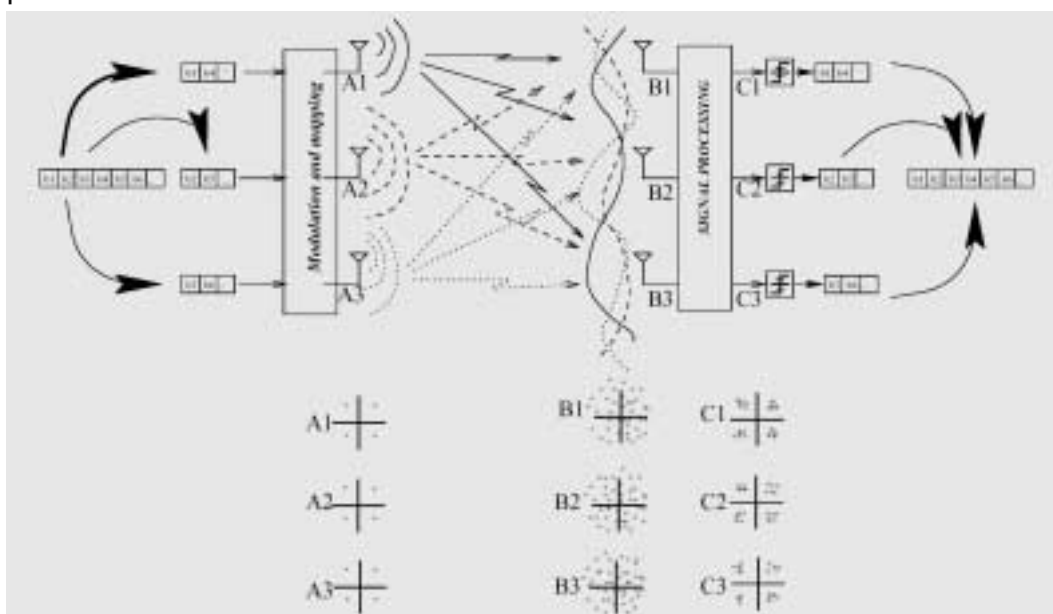


3 Spatial multiplexing

**3 Spatial multiplexing**

**3.1 Principle**

We send multiple signals, the receiver learns the channel matrix and inverts it to separate the data.



**Example for 3x3:**

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix} \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} + \text{Noise}$$

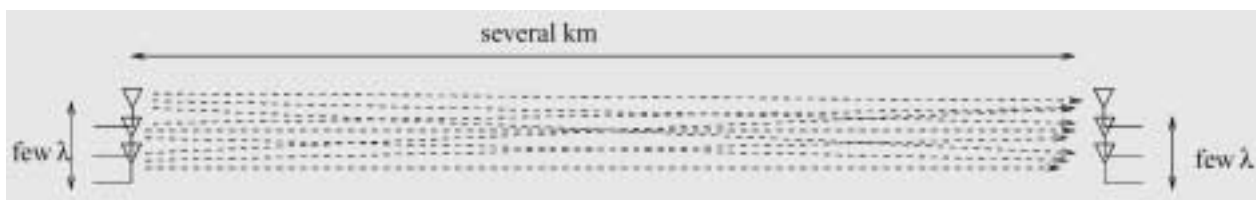
$$\begin{bmatrix} \hat{b}_1 \\ \hat{b}_2 \\ \hat{b}_3 \end{bmatrix} = \mathbf{H}^{-1} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

**3.2 Impact of channel model**

MIMO Performance is very sensitive to channel matrix *invertibility*.

- **The following degrades the conditioning of the channel matrix:**
  - Antenna correlation caused by:**
    - Small antenna spacing, or
    - Small angle spread
- **Line of sight component compared with multipath fading component :**
  - Multipath fading component, close to random identical independent distribution, is well conditioned
  - Line of sight component is very poorly conditioned.

### MIMO spatial multiplexing in Line-of-sight

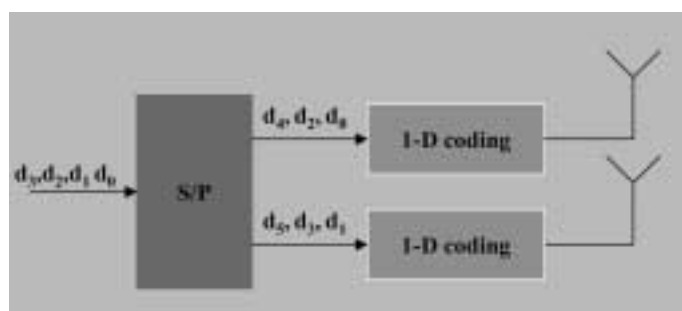


The system  $H \approx \alpha \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$  is near rank one (non invertible) !!

➔ Spatial multiplexing requires multipath to work !!

### 3.3 V-BLAST/ D-BLAST Algorithms

(Bell-labs **L**Ayered **S**pace-**T**ime architecture)  
 Belong to the class of Layered Space-Time Coding



- In D-BLAST, output of coders can be applied to the transmit antennas in turn ➔ Diagonal LST coding (D-BLAST)
- In V-BLAST, output of coders operate co-channel with synchronized symbol timing ➔ Vertical LST coding (V-BLAST)



## 4 MIMO Receiver Design

### 4.1 Linear receivers for BLAST (Zero-Forcing, MMSE)

#### Zero-Forcing receiver

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & \dots \\ h_{21} & h_{22} & \dots \\ \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} S_1 \\ S_2 \\ \vdots \end{bmatrix} + N$$

Zero Forcing implements matrix (pseudo)-inverse (ignores noise enhancement problems):  $\hat{S} = \mathbf{H}^\# \mathbf{X}$

Where:  $\mathbf{H}^\# = (\mathbf{H}^* \mathbf{H})^{-1} \mathbf{H}^*$

#### MMSE receiver

The MMSE (Minimum mean square error) receiver optimizes the following criterion:

$$\mathbf{W} = \operatorname{argmin} \{E |\mathbf{W}^* \mathbf{x} - \mathbf{s}|^2\}$$

We find:

$$\hat{S} = \mathbf{H}^* (\mathbf{H} \mathbf{H}^* + \mathbf{R}_n)^{-1} \mathbf{x}$$

where  $\mathbf{R}_n$  is the noise/intf covariance.

This offers a compromise between residual interference between input signals and noise enhancement.

## 4.2 Non linear receiver (ML, SIC)

### Maximum likelihood receiver:

- Optimum detection
- Exhaustive search. No iterative procedure for MIMO.
- Complexity exponential in QAM order and  $N$ .

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & \dots \\ h_{21} & h_{22} & \dots \\ \vdots & \vdots & \vdots \end{bmatrix} \begin{bmatrix} S_1 \\ S_2 \\ \vdots \end{bmatrix} + N$$

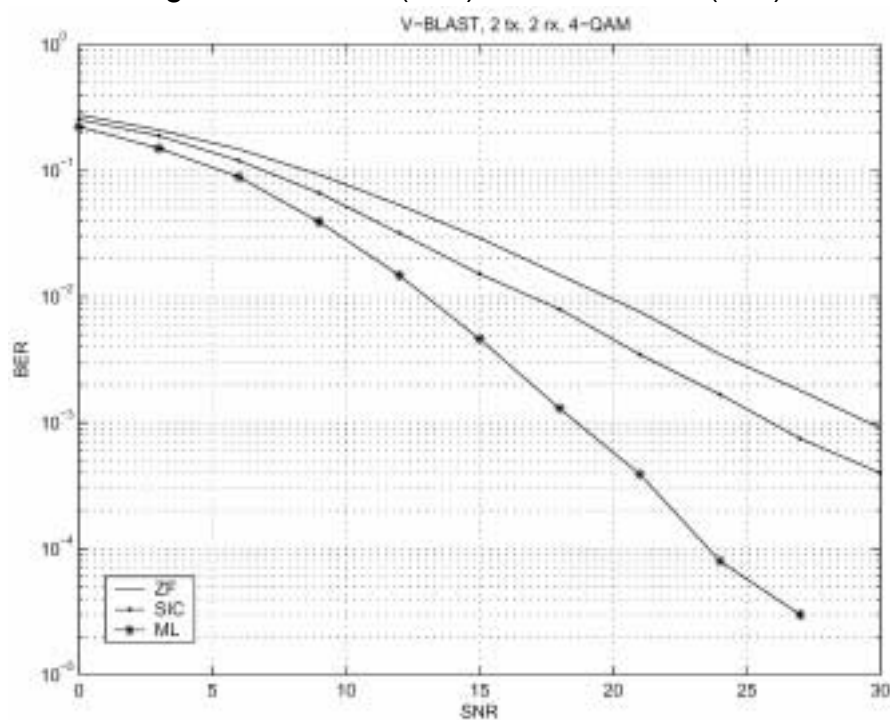
Maximum Likelihood Solution:  $\hat{S} = \operatorname{argmin} \|x - Hs\|^2$

where  $S$  is searched over the modulation alphabet (e.g. 4QAM, 16QAM..)

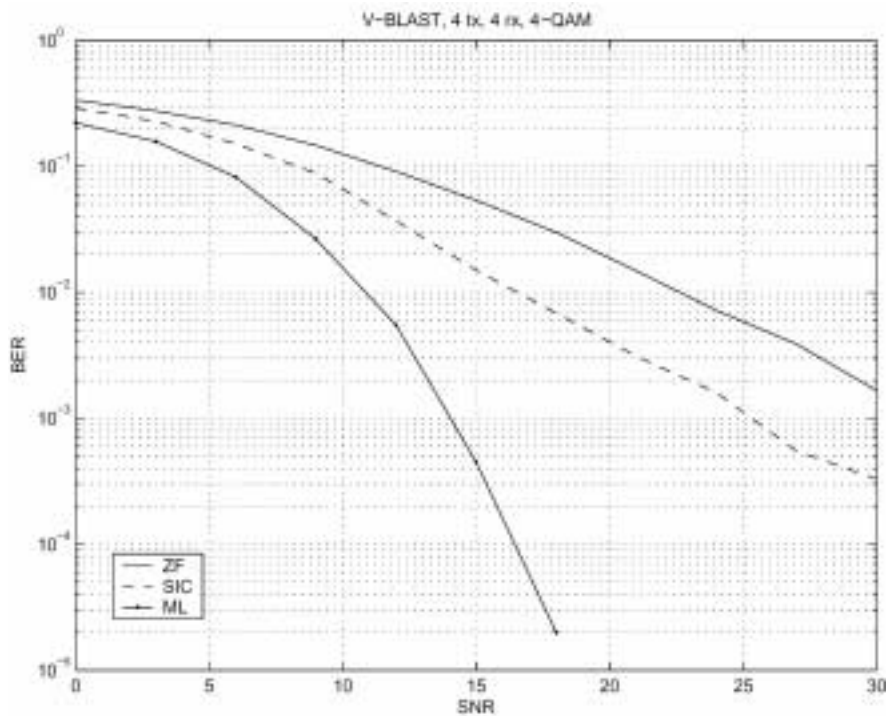
### SIC : Successive Interference Canceling

## 4.3 Performance comparison

BLAST zero-forcing vs. V-BLAST (SIC) vs BLAST-ML (2x2)



### BLAST zero-forcing vs. V-BLAST (SIC) vs BLAST-ML (4x4)



### 5 Space-Time Coding (Transmit / Receive Diversity)

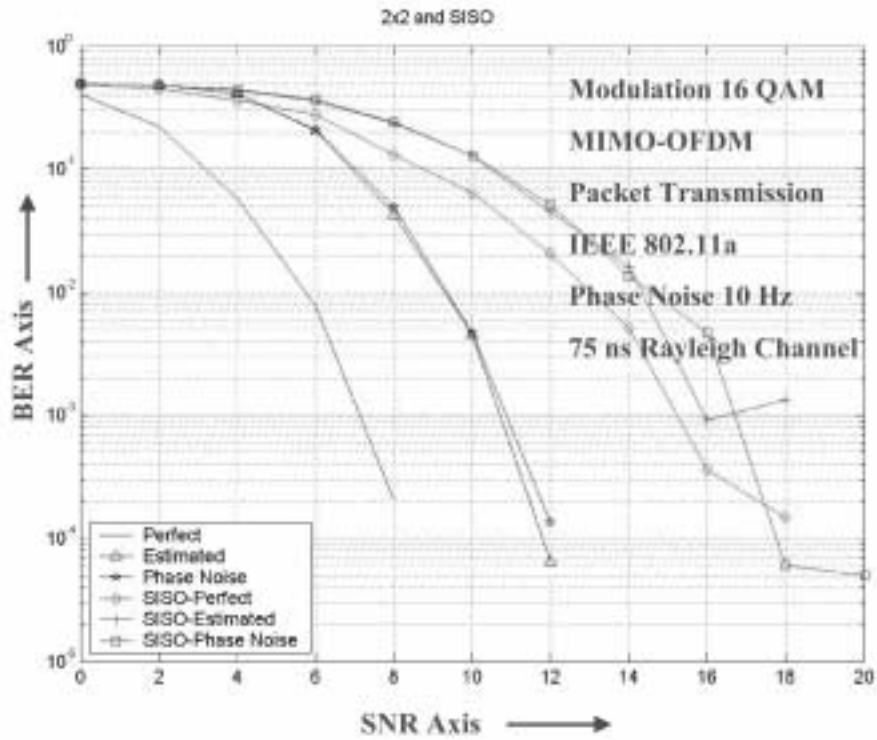
#### **5 Space-Time Coding (Transmit/Receive Diversity)**

Uses Transmission diversity to combat the detrimental effects in wireless fading channels.

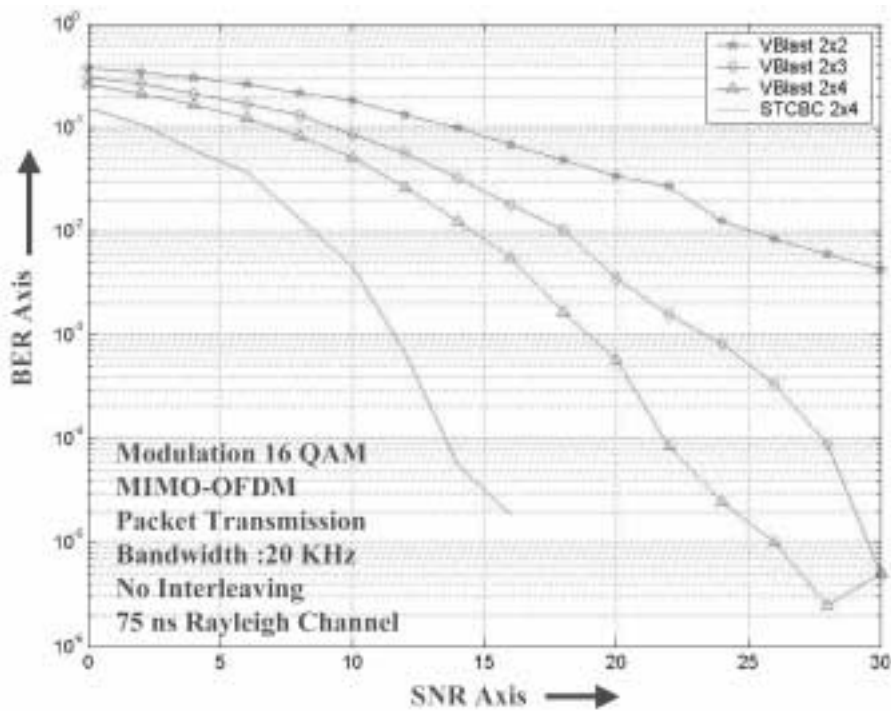
#### **Three types:**

- Trellis space time codes : complex but best performance in slow fading environment (indoors).
- Layered space time codes : easy to implement but not accurate due to error propagation effect.
- Block space time codes** : best trade-off of performance vs complexity.

### Comparison of Performance: 2x2 STCBC and SISO



### Comparison of Performance: V-BLAST & STCBC in MIMO-OFDM



## **Summary : Space-Time Coding & V-BLAST**

### **Space-Time Coding**

- Space-time codes provide spatial diversity gain without requiring channel knowledge in the transmitter
- Space-time codes do not provide array gain (due to lack of channel knowledge in the transmitter)
- Orthogonal space-time codes decouple the vector detection problem into scalar detection problems -> drastically simplified algorithms

### **V-BLAST**

- Performs well when channel estimates are good
- Degradation due to channel estimation errors is fairly high
- Successive Interference Cancellation (SIC) makes for low complexity
- Danger of error propagation that is inherent of a SIC scheme
- Inferior to STBC due to lack of diversity gain at the transmitter

## **6 Conclusion**

**MIMO extremely promising but more validation work are needed :**

### **Algorithms:**

- Unifying diversity and multiplexing approaches
- Optimum loading

### **Low complexity receivers**

- Optimum receivers (ML) are too complex
- Simple receivers (linear) give unacceptable performance at high MIMO loading

### **System gain evaluation**

- Real gains depend on deployment scenario
- Beamforming and MIMO needs to be compared on a system level basis

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## References

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- “An Overview of MIMO Communications- A Key to Gigabit Wireless”, A. J. Paulraj, D. Gore, R. U. Nabar, and H. Bolcskei
- " From theory to practice: An overview of space-time coded MIMO wireless systems " D. Gesbert, M. Shafi, D. Shiu, P. Smith,, *IEEE Journal on Selected Areas on Communications (JSAC)*. April 2003, special issue on MIMO systems. (Recipient of the 2004 IEEE Best Tutorial Paper Award by IEEE Comm. Society).
- “Implementation of a MIMO OFDM-Based Wireless LAN System”, Allert van Zelst, *Student Member, IEEE*, and Tim C. W. Schenk, *Student Member, IEEE*
- “MIMO Systems With Antenna Selection”, Andreas F.Molish, Moe Z.Win

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## Homework

1. Explain the principle of spatial multiplexing.
2. Describe briefly what happens in MIMO spatial multiplexing if there is just line of sight without multipath ?