

Collection of Formulas

$$C = W_C \cdot \log_2(1 + SNR), \begin{cases} r_{\max} = 2B_T = r_b / n = r_b / \log_2(L) \\ \Rightarrow r_b = 2B_T \log_2(L), L = 2^n \end{cases}, r = n \cdot f_S$$

$$C = W_C \cdot \log_2(1 + SNR)$$

$$P_{dB} = 10 \log(P_1 / P_2), P_{dB} = 20 \log(V_1 / V_2), P_{dBm} = 10 \log(P_1 / 1mW), \frac{V_g}{V_i} = \frac{Z_g + Z_L}{Z_L}$$

$$\begin{cases} y(t) = Kx(t - t_d) \\ \Rightarrow Y(f) = F[y(t)] = \underbrace{K \exp(-j\omega t_d)}_{H(f)} X(f), \begin{cases} l = d_{\min} - 1, t = \lfloor l/2 \rfloor, R_C = k/n \leq 1 \\ d_{\min}|_{\max} = n - k + 1 \text{ (repetition codes)} \end{cases} \\ G_y(f) = |H(f)|^2 G_x(f) \text{ (= output PDF)} \end{cases}$$

$$\begin{cases} N_R = \int_{-\infty}^{\infty} (\eta/2) |H_R(f)|^2 df \\ = \int_{B_T} (\eta/2) df + \int_{B_T} (\eta/2) df = \eta B_T \end{cases} \begin{cases} P(n, k) = \binom{n}{k} \alpha^k (1 - \alpha)^{n-k} \\ \binom{n}{k} = \frac{n!}{k!(n-k)!} \end{cases}$$

$$\begin{cases} B_T = 2|D-1|W, 1 \gg D \gg 1 \\ \beta = A_m f_\Delta / f_m |_{A_m=1, f_m=W} = f_\Delta / W \equiv D \\ B_{T,DSB} = 2W, B_{T,SSB} = W \end{cases}$$

$$\begin{cases} x_C(t) = A_C \cos(\omega_C t + \phi(t)) \\ \phi_{PM}(t) = \phi_\Delta x(t) \\ \phi_{FM}(t) = 2\pi f_\Delta \int_{t_0}^t x(\lambda) d\lambda, t \geq t_0 \end{cases} \phi(t) = \begin{cases} \frac{\phi_\Delta A_m}{\beta} \sin(\omega_m t), \text{PM} \\ \frac{(A_m f_\Delta / f_m)}{\beta} \sin(\omega_m t), \text{FM} \end{cases} \begin{cases} \gamma = S_R / (\eta W) \\ S_R / N_R = \gamma W / B_T \\ \gamma_b = E_b / N_0 \end{cases}$$

$$y(t) = \begin{cases} v_i(t) & \text{Synchronous detector} \\ A_v(t) - \overline{A_v} & \text{Envelope detector} \\ \phi_v(t) & \text{Phase detector} \\ d\phi_v(t)/dt & \text{Frequency detector} \end{cases}, \begin{cases} x_{AM}(t) = A_C [1 + \mu x_m(t)] \cos(\omega_c t) \\ x_{DSB}(t) = x_m(t) \cos(\omega_c t) \end{cases}$$

$$\begin{cases} Q = R\sqrt{C/L} \\ f_0 = (2\pi\sqrt{LC})^{-1}, H(\omega) = V_{out}(\omega) / V_{in}(\omega) = z_p / z_i \end{cases}$$

$$Q(k) = \frac{1}{\sqrt{2\pi}} \int_k^\infty \exp\left(-\frac{\lambda^2}{2}\right) d\lambda$$

$$\lambda = (m-x)/\sigma \Rightarrow Q(k) = \frac{1}{\sqrt{2\pi}} \int_{\sigma k+m}^\infty \exp\left(-\frac{(x-m)^2}{2\sigma^2}\right) dx$$

$$\begin{cases} P = UI = U^2/R = I^2 R, & \frac{V_g}{V_i} = \frac{Z_g + Z_L}{Z_L}, P_L = V_i I_i \cos \theta \\ R = U/I \end{cases}$$

$$\cos \theta = R_{tot}/Z_{tot} = R_{tot}/\sqrt{R_{tot}^2 + X_{tot}^2}, X_{tot} = X_g + X_L, R_{tot} = R_L + R_g$$

$$N_{D(PM)} = \int_{-W}^W \frac{\eta}{2S_R} df = \frac{\eta W}{S_R}, N_{D(FM)} = \int_{-W}^W \frac{\eta f^2}{2S_R} df = \frac{\eta W^3}{3S_R}$$

$$S_D/N_D|_{FM} = \frac{f_\Delta^2 S_x}{\eta W^3/(3S_R)} = 3 \underbrace{\left(\frac{f_\Delta}{W}\right)^2}_D S_x \underbrace{\frac{S_R}{\eta W}}_\gamma = 3D^2 S_x \gamma, S_D/N_D|_{FM, D \gg 1} = \frac{3}{4} \left(\frac{B_T}{W}\right)^2 S_x \gamma$$

$$S_D/N_D|_{PM} = \frac{\phi_\Delta^2 S_x}{\eta W/S_R} = \phi_\Delta^2 S_x \gamma, \text{ where } \phi_\Delta^2 S_x \leq \pi^2$$

$$\begin{cases} \int \frac{1}{1+x^2} dx = \arctan(x) & \left\{ \Pi\left(\frac{t}{\tau}\right) \leftrightarrow \tau \operatorname{sinc} f\tau \right. \\ \int \frac{x^2}{1+x^2} dx = x - \arctan(x) & \left. \Lambda\left(\frac{t}{\tau}\right) \leftrightarrow \tau \operatorname{sinc}^2 f\tau \right. \end{cases}$$

$$\begin{cases} \frac{d^n v(t)}{dt^n} \leftrightarrow (j2\pi f)^n V(f) \\ \int_{-\infty}^t v(\lambda) d\lambda \leftrightarrow \frac{1}{j2\pi f} V(f) + \frac{1}{2} V(0) \delta(f) \end{cases}$$

$$\begin{cases} \sin \alpha \sin \beta = 1/2 \cos(\alpha - \beta) - 1/2 \cos(\alpha + \beta) \\ \cos \alpha \cos \beta = 1/2 \cos(\alpha - \beta) + 1/2 \cos(\alpha + \beta), \\ \sin \alpha \cos \beta = 1/2 \sin(\alpha - \beta) + 1/2 \sin(\alpha + \beta) \end{cases} \begin{cases} \cos^2 \alpha = (1 + \cos 2\alpha)/2 \\ \cos^3 \alpha = (3 \cos \alpha + \cos 3\alpha)/4 \\ (\alpha + \beta)^2 = \alpha^2 + 2\alpha\beta + \beta^2 \\ (\alpha + \beta)^3 = \alpha^3 + 3\alpha^2\beta + 3\alpha\beta^2 + \beta^3 \end{cases}$$

