

S-72.3275 Cellular Radio Network Planning and Optimization

Exercise Set 1

Solutions

Spreading and Modulation 1

A direct sequence spread-spectrum system is used to resolve the multipath signal components in a two-path radio signal propagation scenario. If the path length of the secondary path is 300 m longer than that of the direct path, determine the minimum chip rate necessary to resolve the multipath components. How would WCDMA cope with this situation?

[If the two paths would be received within a time interval of one chip, the paths could not be resolved; hence only one rake-finger would be allocated to the paths. To be able to distinguish between the paths, the chip time T_{chip} has to be

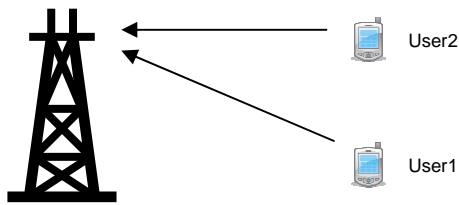
$$T_{chip} = \frac{\Delta d}{c} = \frac{300 \text{ m}}{3 \cdot 10^8 \text{ m/s}} = 1 \text{ } \mu\text{s}$$

$$\Rightarrow R = \frac{1}{T_{chip}} = 1 \text{ Mcps}$$

WCDMA chip rate = $3.84 \cdot 10^6$, hence it can resolve path length differences bigger than 78.1 m. This is a good value to keep in mind!]

Spreading and Modulation 2

Consider the uplink of a CDMA system with two synchronous users received as shown in picture below.



User 1 spreads its bipolar data signal d_1 with the sequence $C_1 = [-1 -1 -1 +1 -1 +1 +1 +1]$.
 User 2 spreads its data signal $d_2 \in \{-1, +1\}$ with the sequence $C_2 = [+1 +1 -1 +1 +1 -1 -1 -1]$.
 The received values for the chips of the first bit are $y = [00 -22 0000]$.

1. What is the spreading factor? What is the spreading gain in dB?

[SF=8, spreading gain=9dB]

2. Are these sequences C_1 and C_2 orthogonal to each other?

[$C_1 * C_2^T = -4$, signals not orthogonal]

3. Perform the despreading operation for the first bit of user 1. What is the estimated bit?

[Result of despreading: 4, estimated bit: +1]

4. Perform the despreading operation for the first bit of user 2. What is the estimated bit?

[Result of despreading: 4, estimated bit: +1]

5. Determine the SIR for user 1.

$$\left[SIR_1 = \frac{|ACF_1(0)|^2}{|CCF(0)|} = \frac{|8|^2}{|4|} = 4 = 6\text{dB} \right]$$

6. What would be the SNR if the distortion to user 1 would be thermal noise (instead of user 2) with the same power?

[SNR = SF in decibel domain $10 * \log(SF)$]

7. Why is there a difference between the SNR and the SIR values? What is the possible range of SIR values?

[SIR depends on the CCF between the two sequences; possible range: 0dB (identical sequences) .. +inf dB (orthogonal sequences).]

Spreading and Modulation 3

Consider the uplink of W-CDMA. Given a spreading factor of 64 for DPDCH and 256 for DPCCH, an information bitrate of 15.6 kbps (12.2 kbps + 3.4 kbps for data and control correspondingly), and a power ratio of 1/9 between control and data channel:

1. What is the symbol rate for DPDCH?

$$\left[\text{symbol rate} = \frac{W}{SF} = \frac{3840 \text{ Mcps}}{64} = 60 \text{ ksym/s} \right]$$

2. What is the spreading gain for DPDCH in dB?

$$[10 \log(SF) = 18.1 \text{ dB}]$$

3. What is the processing gain considering the whole transmission?

$$\left[PG = 10 \log \left(\frac{W}{R_{info}} \right) = 23.9 \text{ dB} \right]$$

[Here R_{info} is naturally the whole information bitrate, including control information!]

4. Give the relation between SNR, CINR and PG.

$$[SNR = CINR + PG]$$

5. A practical task where you utilize your expertise gained from solving last four problems:

In our example now, a reliable signal reception requires $E_b/N_0 = 5 \text{ dB}$. The properties of DPDCH and DPCCH remain the same. Assuming a noise floor of -103 dBm , what is the required signal strength of the whole signal at the Node B receiving end? Consider the signal as whole, do not separate data and control parts.

$$\begin{aligned} P_{RxMin} &= P_{n+I} + E_c/N_0 \\ &= P_{n+I} + (E_b/N_0 - PG) \\ &= -103 \text{ dBm} + (5 \text{ dB} - 23.9 \text{ dB}) \\ &= -121.9 \text{ dBm} \end{aligned}$$

What is the required RX power of DPCCH?

[Relation between data and control = 1/9]

$$\begin{aligned} \Rightarrow \text{DPDCH power} &= 9/10 * \text{total power} \\ \Rightarrow \text{DPCCH power} &= 1/10 * \text{total power} \\ \Rightarrow P_{RxMin, dpch} &= P_{RxMin} - 10 \text{ dB} = -131.9 \text{ dBm} \end{aligned}$$

Spreading and Modulation 4

Consider the uplink of a WCDMA system. There are 15 users transmitting information bits at a rate of 12,2 kbps. The required E_b/N_0 to achieve sufficient performance is 6 dB. All users are received with equal power of 1 mW. The thermal noise power at the receiver is 5 mW.

1. Determine the carrier-to-interferer-and-noise ratio CINR at the receiver.

$$[CINR = 1 \text{ mW} / (14 \text{ mW} + 5 \text{ mW}) = 1/19 = -12.8 \text{ dB}]$$

2. What is the processing gain?

$$[PG = \text{chip_rate} / \text{bit_rate} = 3.84 \text{ Mcps} / 12.2 \text{ kbps} = 25 \text{ dB}]$$

3. Is the E_b/N_0 value sufficient?

$$[E_b/N_0 = CINR + PG = 12.2 \text{ dB} > 6 \text{ dB} \Rightarrow E_b/N_0 \text{ value is sufficient!}]$$

4. What is the minimum receive power per user such that the required E_b/N_0 is satisfied? (still all users are received with the same power)

$$\left[\begin{array}{l} \text{Minimum required CINR} = E_b/N_0 - PG = -19 \text{ dB} \quad B = 0,0126 \\ \text{Let } x \text{ denote the minimum receive power per user:} \\ \frac{x}{14x + 5 \text{ mW}} = 0,0126 \Rightarrow x = 0,076 \text{ mW} \end{array} \right]$$

5. What is the maximum number of users that can be received with sufficient performance if an infinite receive power is allowed (pole capacity)?

$$\left[\begin{array}{l} \text{Infinite receive power} \Rightarrow \text{thermal noise power can be neglected.} \\ \frac{x}{(a-1)x} = 0,0126 \Rightarrow a = 1/0,0126 + 1 = 80 \end{array} \right]$$

6. How much should the processing gain be increased to allow for doubling the number of users?

[3 dB, remember that WCDMA is a typical case of interference limited capacity.

Doubling the amount of users is possible either by

1. Implementing a system that supports the considered service with 3 dB less E_b/N_0 , or
2. Implementing a system that needs for considered service "3 dB" less information bit rate yielding doubled processing gain.]